

**POLARES****CARACOLES**

|                                                                                                      |
|------------------------------------------------------------------------------------------------------|
| $r = a \pm b \cos(\theta) \quad \text{o} \quad r = a \pm b \sin(\theta) \quad ; a > 0 ; \quad b > 0$ |
|------------------------------------------------------------------------------------------------------|

**SIMETRÍAS:**

$r = a + b \cos(\theta)$       simetría con respecto al eje polar, apunta a 0

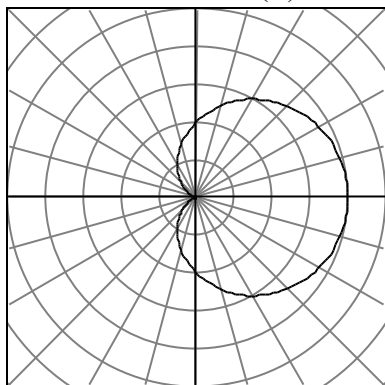
$r = a - b \cos(\theta)$       simetría con respecto al eje polar, apunta a  $\pi$

$r = a + b \sin(\theta)$       simetría con respecto a  $\frac{\pi}{2}$ , apunta a  $\frac{\pi}{2}$

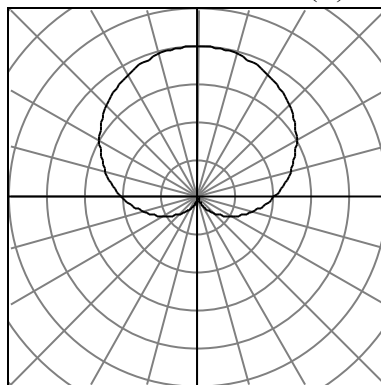
$r = a - b \sin(\theta)$       simetría con respecto a  $\frac{\pi}{2}$ , apunta a  $\frac{3\pi}{2}$

**1) Si  $\frac{a}{b} = 1$       Cardioide**

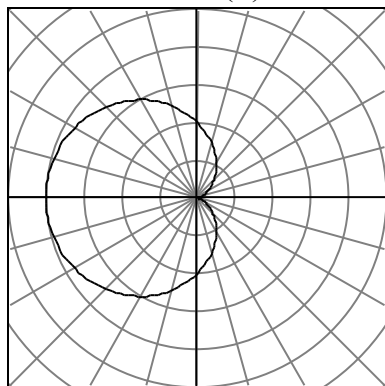
$$r = 2 + 2 \cos(\theta)$$



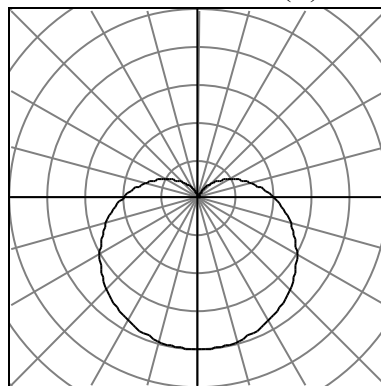
$$r = 2 + 2 \sin(\theta)$$



$$r = 2 - 2 \cos(\theta)$$

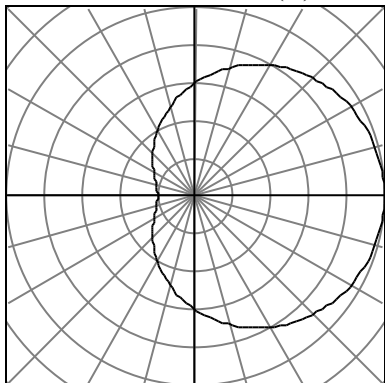


$$r = 2 - 2 \sin(\theta)$$

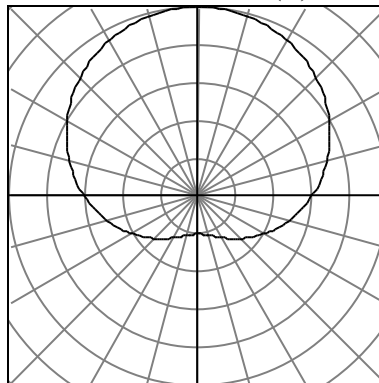


2) Si  $1 < \frac{a}{b} < 2$  **Caracol con hendidura**

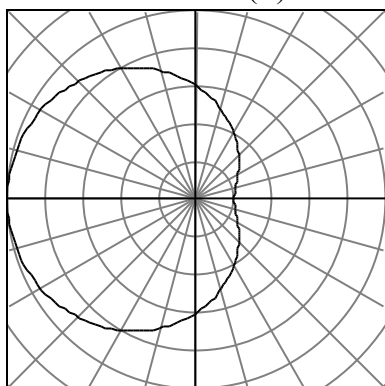
$$r = 3 + 2 \cos(\theta)$$



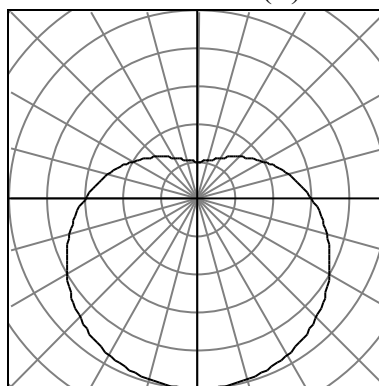
$$r = 3 + 2 \sin(\theta)$$



$$r = 3 - 2 \cos(\theta)$$

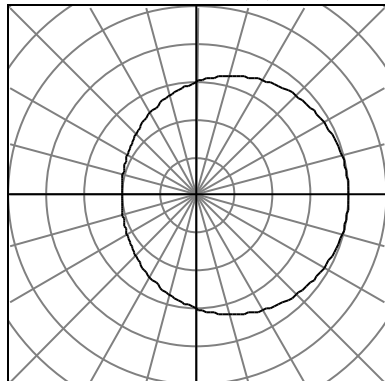


$$r = 3 - 2 \sin(\theta)$$

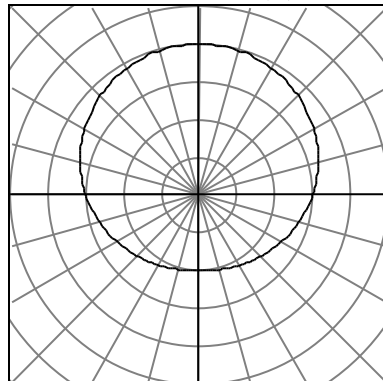


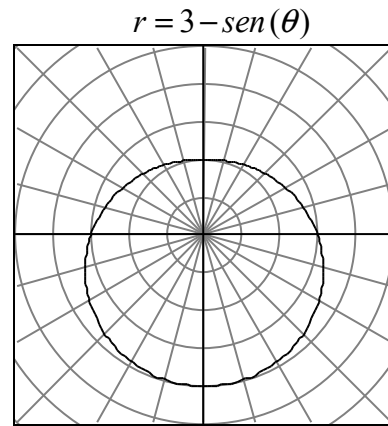
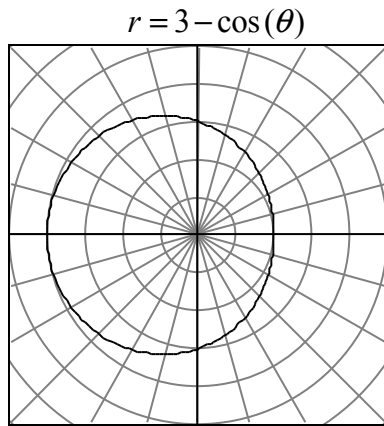
3) Si  $2 \leq \frac{a}{b}$  **Caracol convexo**

$$r = 3 + \cos(\theta)$$



$$r = 3 + \sin(\theta)$$





### **ROSAS O ROSETAS**

$$r = a \cos(n\theta) \quad \text{o} \quad r = a \sin(n\theta) \quad ; \quad \text{n}^\circ \text{ de hojas} \begin{cases} n & ; n \text{ impar} \\ 2n & ; n \text{ par} \end{cases}$$

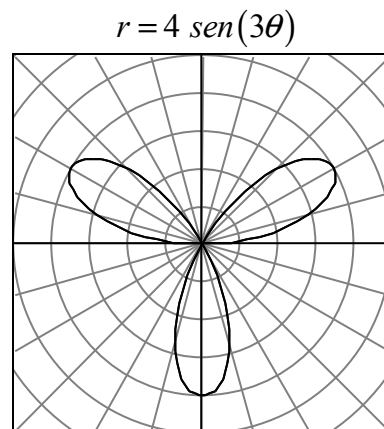
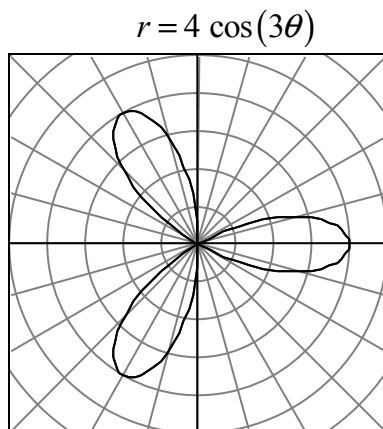
#### **SIMETRÍAS:**

Si  $n$  par ;  $r = a \cos(n\theta)$  simetría con respecto al eje polar, al polo; a  $\frac{\pi}{2}$ .

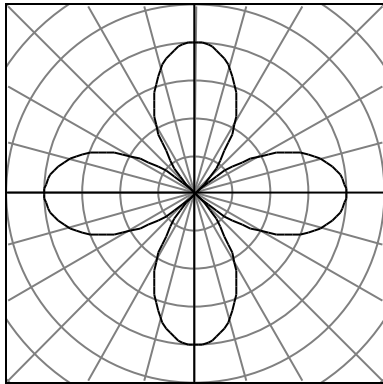
Si  $n$  impar;  $r = a \cos(n\theta)$  simetría con respecto al eje polar.

Si  $n$  par ;  $r = a \sin(n\theta)$  simetría con respecto al eje polar, al polo; a

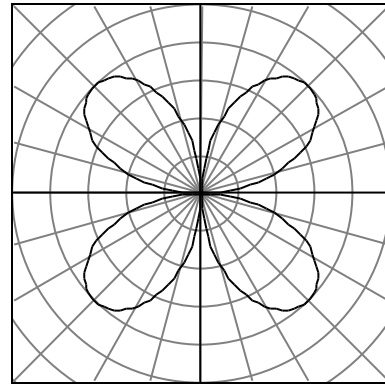
Si  $n$  impar;  $r = a \sin(n\theta)$  simetría con respecto a  $\frac{\pi}{2}$



$$r = 4 \cos(2\theta)$$



$$r = 4 \operatorname{sen}(2\theta)$$



### CIRCUNFERENCIAS

$$r = a \cos(\theta) \quad \text{o} \quad r = a \operatorname{sen}(\theta)$$

#### SIMETRÍAS:

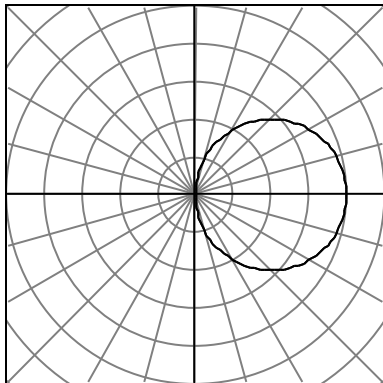
Si  $a > 0$  ;  $r = a \cos(\theta)$  simetría con respecto al eje polar, apunta a 0

Si  $a < 0$  ;  $r = a \cos(\theta)$  simetría con respecto al eje polar, apunta a  $\pi$

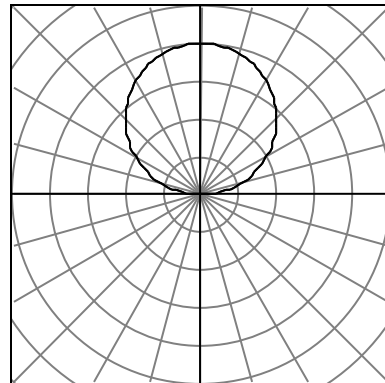
Si  $a > 0$  ;  $r = a \operatorname{sen}(\theta)$  simetría con respecto a  $\frac{\pi}{2}$ , apunta a  $\frac{\pi}{2}$

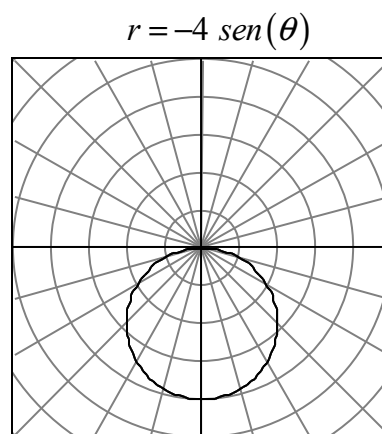
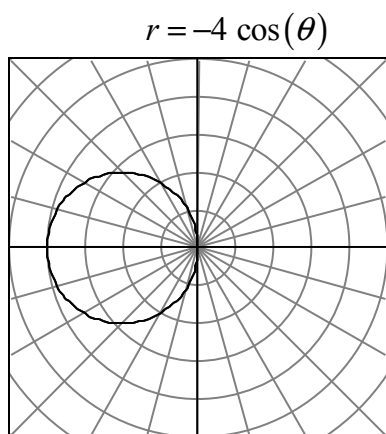
Si  $a < 0$  ;  $r = a \operatorname{sen}(\theta)$  simetría con respecto a  $\frac{\pi}{2}$ , apunta a  $\frac{3\pi}{2}$

$$r = 4 \cos(\theta)$$



$$r = 4 \operatorname{sen}(\theta)$$





### LEMNISCATAS

$$r^2 = a^2 \cos(2\theta) \quad \text{o} \quad r^2 = a^2 \operatorname{sen}(2\theta)$$

SIMETRÍAS:

$r^2 = a^2 \cos(2\theta)$  simetría con respecto al eje polar

$r^2 = a^2 \operatorname{sen}(2\theta)$  simetría al polo.

