

Prueba N°5 Matemáticas:

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Pregunta 1: $y = \sin(\ln x) + \cos(\ln x)$

$$\frac{d^2 y}{dx^2} \cdot x^2 + \frac{dy}{dx} \cdot x + y = 0.$$

$$y' = \frac{\cos(\ln(x))}{x} + \frac{(-\sin(\ln(x)))}{x} = \frac{\cos(\ln(x)) - \sin(\ln(x))}{x}$$

$$y'' = \frac{(\cos(\ln(x)) - \sin(\ln(x)))' \cdot x - (\cos(\ln(x)) - \sin(\ln(x))) \cdot 1}{x^2}$$

$$y'' = \frac{-2 \cos(\ln(x))}{x^2}$$

$$\frac{-2 \cos(\ln(x))}{x^2} \cdot x^2 + \frac{\cos(\ln(x)) - \sin(\ln(x))}{x} \cdot x + \sin(\ln(x)) + \cos(\ln(x)) = 0$$

$$-2 \cos(\ln(x)) + \cos(\ln(x)) - \sin(\ln(x)) + \sin(\ln(x)) + \cos(\ln(x)) = 0$$

$$-2 \cos(\ln(x)) + \cos(\ln(x)) + \cos(\ln(x)) = 0$$

$$-2 \cos(\ln(x)) + 2 \cos(\ln(x)) = 0$$

$$0 = 0$$

Pregunta 2: $\frac{dy}{dx}$

a) $y = 3 \tan(x^3 + x) / \ln$

$$\ln(y) = \tan(x^3 + x) \cdot \ln(3)$$

$$\frac{y'}{y} = \sec^2(x^3 + x) \cdot (3x^2 + 1) \cdot \ln(3) \quad \left\downarrow \frac{d}{dy}\right.$$

● $y' = 3 \tan(x^3 + x) \cdot \sec^2(x^3 + x) \cdot (3x^2 + 1) \cdot \ln(3)$

b) $y = \frac{(e^x - x)^{10} \cdot (8 + x^3)^2}{\sqrt{6 + \sqrt{x}}} \cdot \ln$
 $\sqrt{6 + \sqrt{x}} \rightarrow (6 + \sqrt{x})^{1/2}$

$$\ln(y) = \frac{10 \ln(e^x - x) + 2 \ln(8 + x^3)}{1/2 \ln(6 + \sqrt{x})}$$

$$\sqrt{x} = x^{1/2}$$

$$\ln(y) = (10 \ln(e^x - x) + 2 \ln(8 + x^3)) - (1/2 \ln(6 + \sqrt{x})) \quad \left\downarrow \frac{d}{dy}\right.$$

● $\frac{y'}{y} = 10 \cdot \frac{1}{(e^x - x)} \cdot (e^x - 1) + 2 \cdot \frac{1}{(8 + x^3)} \cdot 3x^2 - \left(\frac{1}{2} \cdot \frac{1}{6 + \sqrt{x}} \cdot \frac{1}{2\sqrt{x}} \right)$

$$y' = \left(\frac{10(e^x - 1)}{(e^x - x)} + \frac{6x^2}{(8 + x^3)} - \frac{1}{2(6 + \sqrt{x})(2\sqrt{x})} \right) \left(\frac{(e^x - x)^{10} \cdot (8 + x^3)^2}{\sqrt{6 + \sqrt{x}}} \right)$$

Pregunta 2:

c)

$$y = \frac{\operatorname{Sen}(x) \cdot (x^2 + x)^{3x}}{110} \quad / \ln$$

$$\ln(y) = \frac{\ln(\operatorname{Sen}(x)) \cdot 3x \ln(x^2 + x)}{\ln(110)}$$

$$\ln(y) = (\ln(\operatorname{Sen}(x)) + 3x \cdot \ln(x^2 + x)) - \ln(110) \quad \downarrow \frac{d}{dx}$$

$$\frac{y'}{y} = \frac{1}{\operatorname{Sen}(x)} \cdot \cos(x) + 3 \ln(x^2 + x) + 3x \cdot \frac{1}{x^2 + x} (2x + 1) - 0$$

$$y' = \left(\frac{\cos(x)}{\operatorname{Sen}(x)} + 3 \ln(x^2 + x) + \frac{3x(2x + 1)}{x^2 + x} \right) \cdot \left(\frac{\operatorname{Sen}(x) \cdot (x^2 + x)^{3x}}{110} \right)$$

Pregunta 3:

a) $y^2 = x^3 + \cos(xy) - x \ln(y) \rightarrow \frac{dy}{dx}$

$$2y \cdot y' = 3x^2 + \cos(xy) \cdot (y + xy') - (\ln(y) + x \cdot \frac{1}{y} \cdot y')$$

$$2y \cdot y' + \frac{x}{y} \cdot y' - \cos(xy) \cdot (xy') = 3x^2 - \ln(y) + \cos(xy) \cdot y$$

$$y' (2y + \frac{x}{y} - \cos(xy) \cdot x) = 3x^2 - \ln(y)$$

$$y' = \frac{(3x^2 - \ln(y)) + \cos(xy) \cdot y}{2y + \frac{x}{y} - \cos(xy) \cdot x}$$

b) $y + x \cdot \sqrt{1+2y} = x^2 \rightarrow y'(1,0)$

$$y' + \sqrt{1+2y} + x \cdot \frac{1}{2\sqrt{1+2y}} \cdot 2y' = 2x$$

$$y' + \sqrt{1+2 \cdot 0} + 1 \cdot \frac{1}{2\sqrt{1+2 \cdot 0}} \cdot 2y' = 2 \cdot 1$$

$$y' + \sqrt{1+0} + 1 \cdot \frac{1}{2\sqrt{1+0}} \cdot 2y' = 2$$

$$y' + 1 + 1 \cdot \frac{1}{2} \cdot 2y' = 2$$

$$y' + 1 + 1 \cdot y' = 2$$

$$y' + y' = 2 - 1$$

$$2y' = 1$$

$$y' = \frac{1}{2}$$

Pregunta 4:

a) $3x^2y + y^2 - 3x = 1$ $P(1, -4)$ tangente.

$$6xy + 3x^2 \cdot y' + 2y \cdot y' - 3 = 0$$

$$6 \cdot 1 \cdot -4 + 3 \cdot (1)^2 \cdot y' + 2 \cdot -4 \cdot y' - 3 = 0.$$

$$6 \cdot -4 + 3 \cdot 1 \cdot y' + (-8) \cdot y' - 3 = 0.$$

$$\underline{-24 + 3 \cdot y' - 8 \cdot y' - 3 = 0}$$

$$\underline{-27 + 3y' - 8y' = 0}$$

$$\underline{-27 - 5y' = 0}$$

$$\underline{\frac{-27}{5} = 5y'}$$

$$y + 4 = \underline{\frac{-27}{5}} (x - 1)$$

$$y = \underline{\frac{-27}{5}} x + \underline{\frac{27}{5}} - 4$$

$$y + 4 = \underline{\frac{-27}{5}} (x - 1)$$

$$y = \underline{\frac{-27}{5}} x + \underline{\frac{27}{5}} - 4$$

$$y = \underline{\frac{-27}{5}} x + \underline{\frac{27}{5}} - \underline{\frac{20}{5}}$$

$$y = \underline{\frac{-27}{5}} x + \underline{\frac{7}{5}}$$

Pregunta 4:

b) $f(x) = x^3 - 8x + 2$ $m+ = 4$ normal.

$$y' = 3x^2 - 8$$

$$4 = 3x^2 - 8$$

$$4 + 8 = 3x^2$$

$$\frac{12}{3} = 3x^2$$

$$4 = x^2$$

$$4 = x^2 \quad \sqrt{\quad}$$

$$x = \pm 2$$

$$y = (2)^2 - 8 \cdot 2 + 2$$

$$y = 8 - 16 + 2$$

$$y = -6$$

$$1) P(2, -6)$$

$$y = (-2)^2 - 8 \cdot (-2) + 2$$

$$y = 8 + 16 + 2$$

$$y = 26$$

$$2) P(-2, 26)$$

$$1) y - (-6) = -1/4 (x - 2)$$

$$y + 6 = -1/4 x + 1/2$$

$$y = -1/4 x - 11/2$$

$$2) y - 26 = -1/4 (x + 2)$$

$$y = -1/4 x - 1/2 + 26$$

$$y = -1/4 x + 25/2$$